



第四章 CMOS单元电路

4.1 反相器直流特性

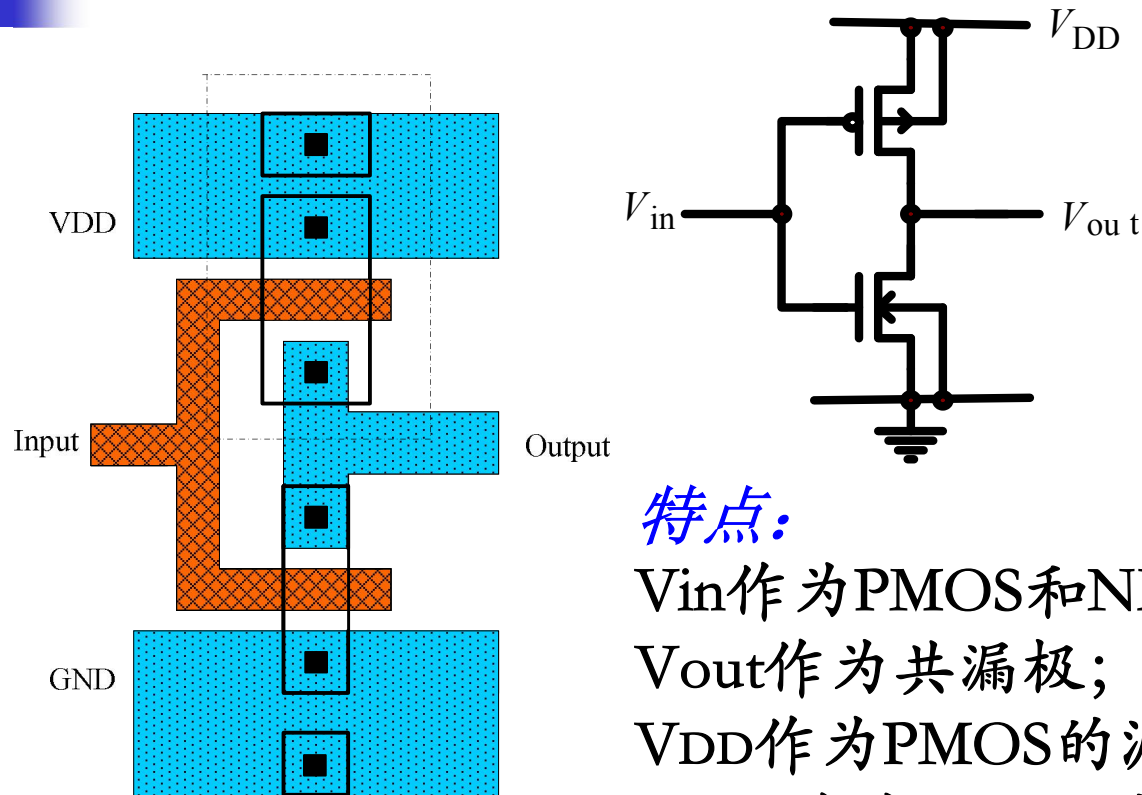
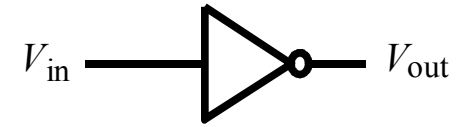


CMOS反相器

- **4.1 CMOS反相器的直流特性**
- **4.2 CMOS反相器的瞬态特性**
- **4.3 CMOS反相器的设计**

CMOS Inverter

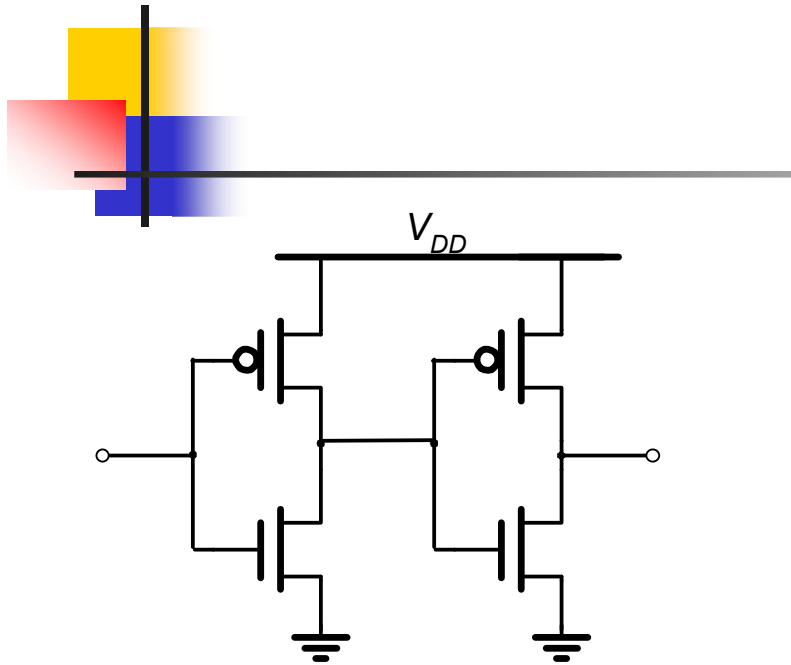
反相器的逻辑符号



特点:

- V_{in} 作为PMOS和NMOS的共栅极;
- V_{out} 作为共漏极;
- V_{DD} 作为PMOS的源极和体端;
- GND 作为NMOS的源极和体端

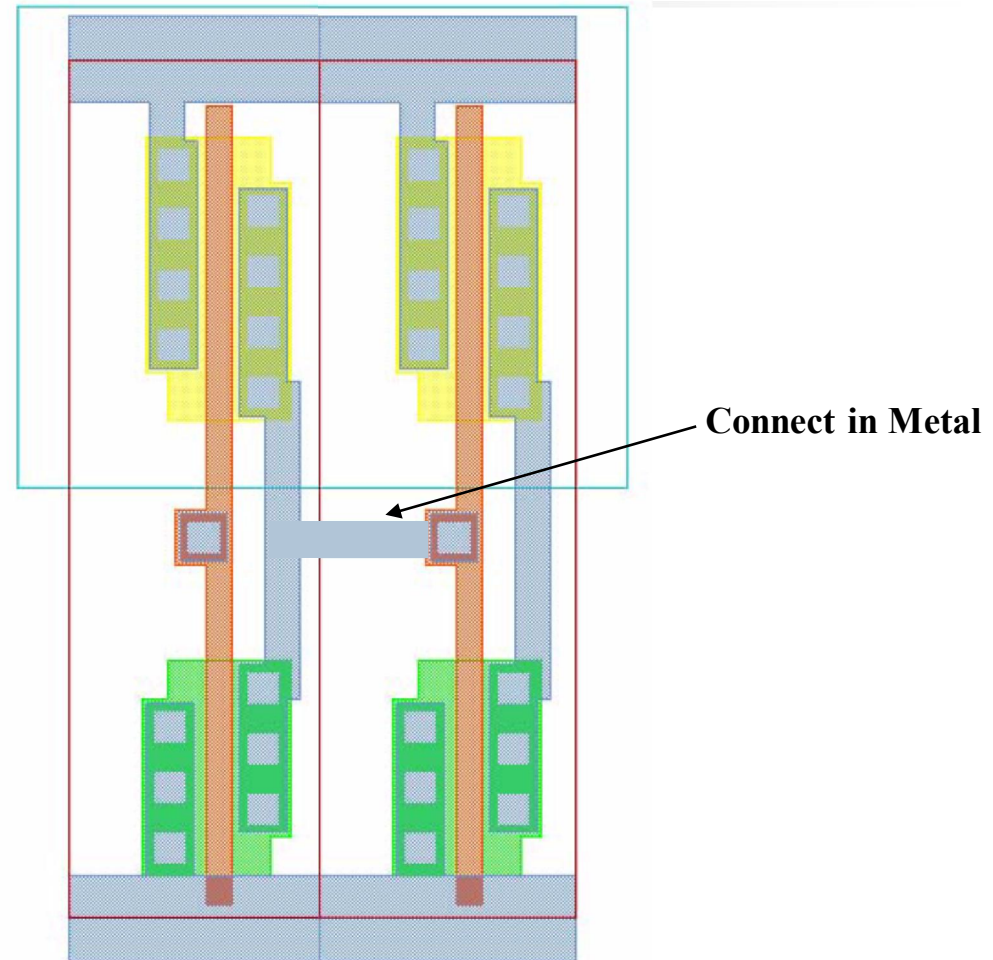
Two Inverters



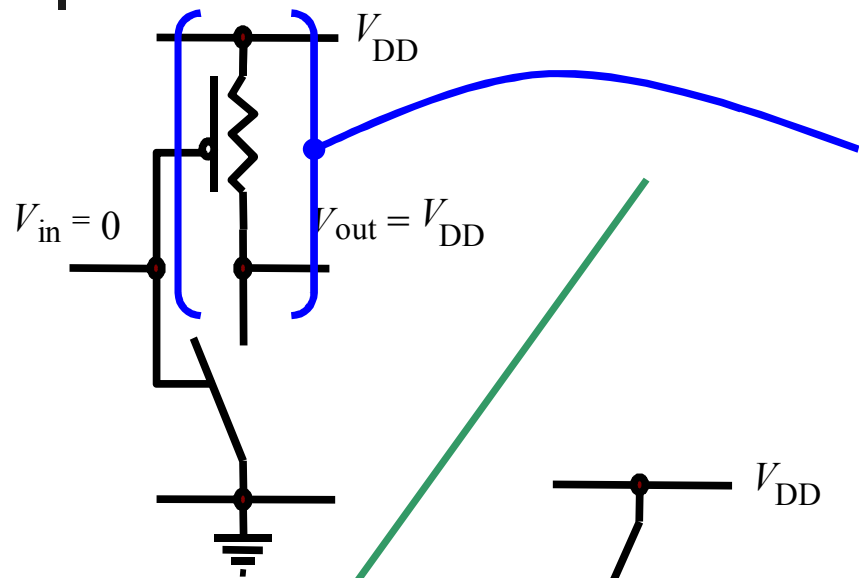
- 标准单元形式的门电路的版图设计
- 通过等高的设计共享电源和地线
- 通过邻接的设计减小面积

Share power and ground

Abut cells



CMOS反相器的直流特性



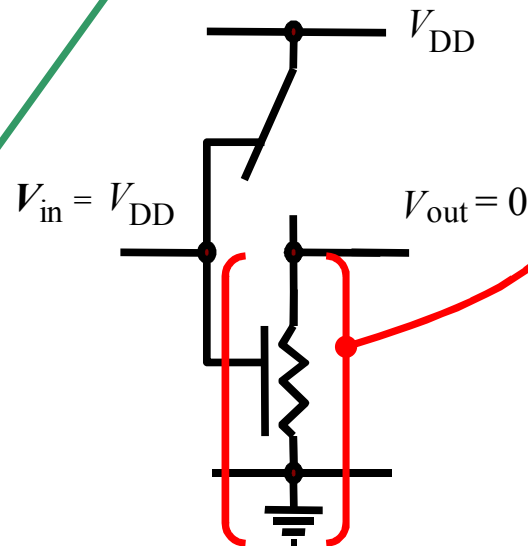
✓ $V_{in} = 0$, NMOS截止, PMOS导通,
稳态 $V_{out} = V_{DD}$, “1”;

✓ $V_{in} = V_{DD}$, NMOS导通, PMOS截止,
稳态 $V_{out} = 0$;

反相器的工作特点:

✓ **$V_{out} = \overline{V_{in}}$** ;

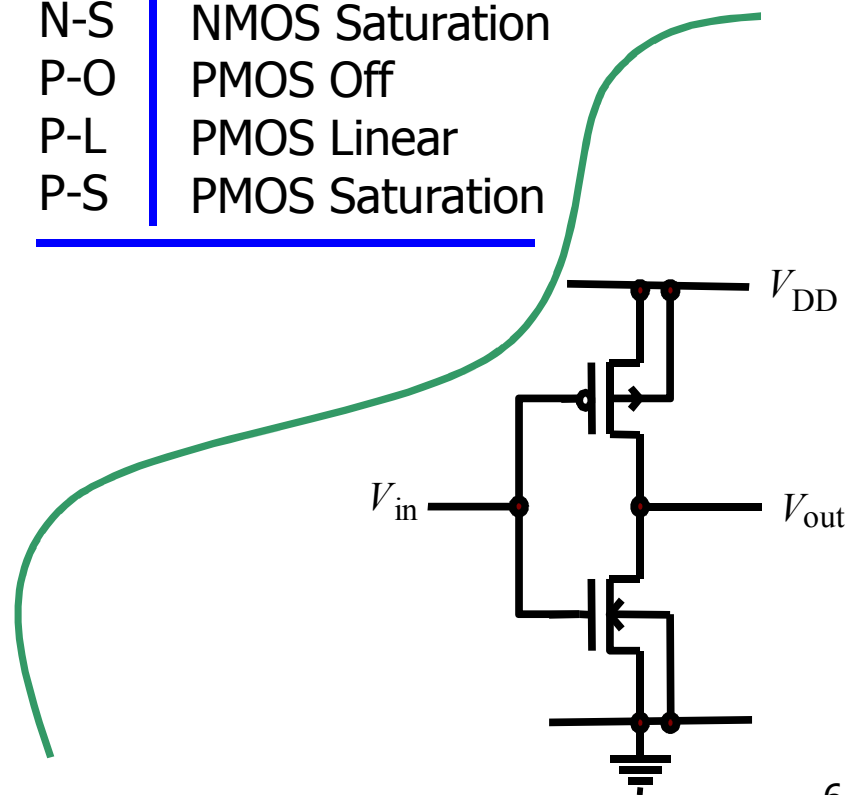
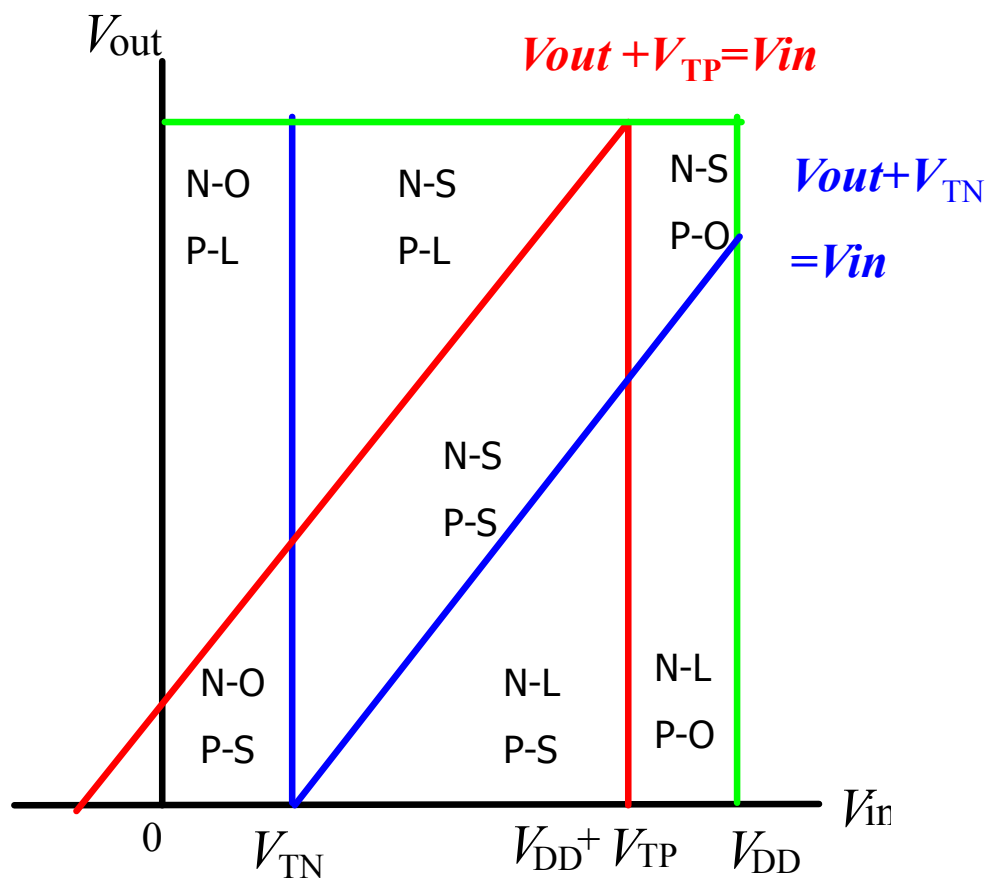
✓ 稳态单管导通, 没有直通电流



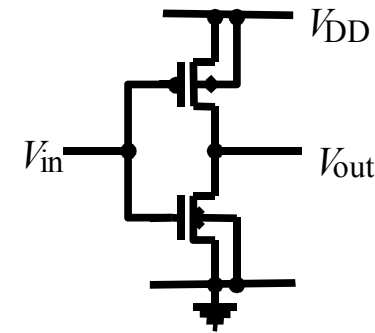
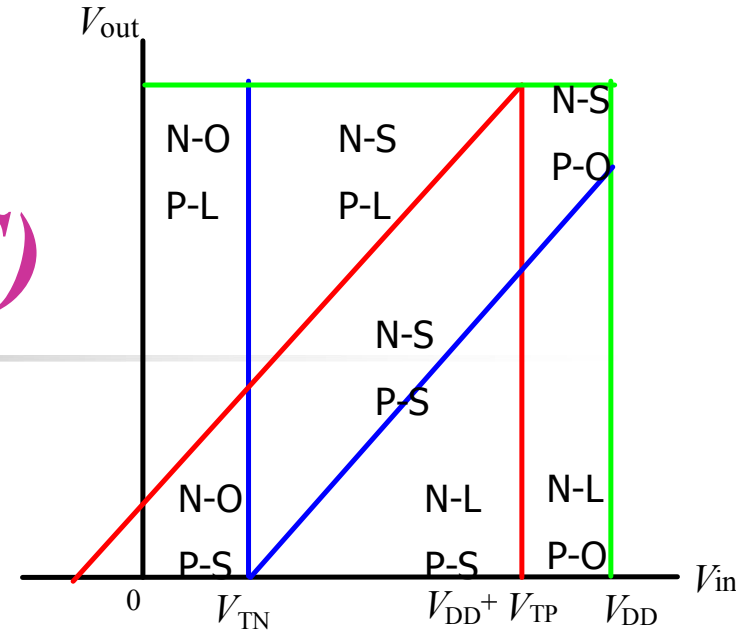
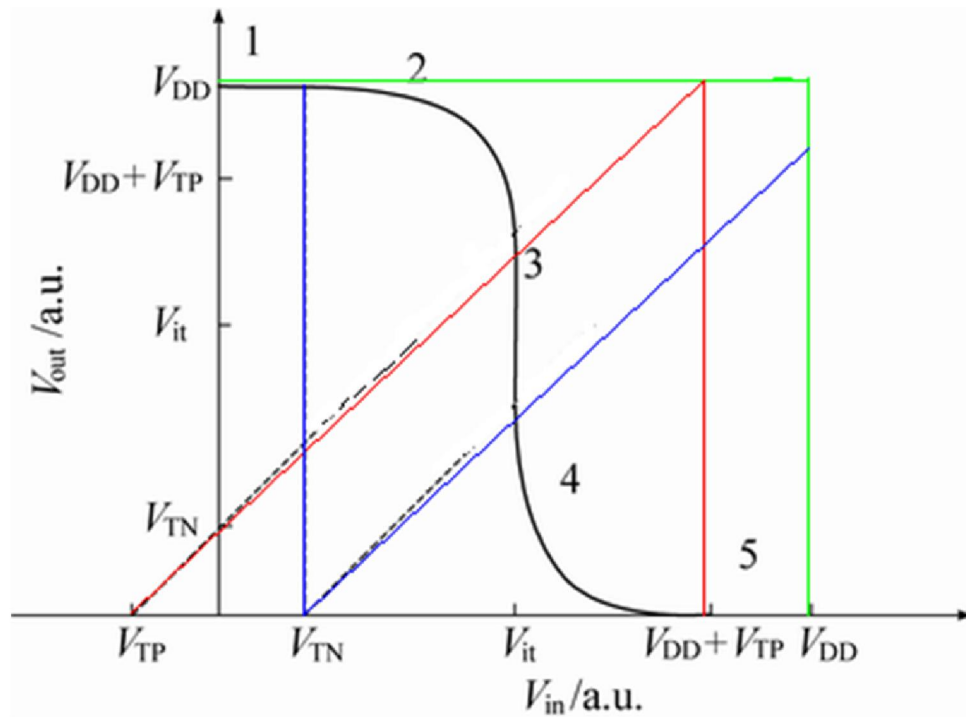
反相器中 *MOSFET* 的工作区域

缩写对照:

N-O	NMOS Off
N-L	NMOS Linear
N-S	NMOS Saturation
P-O	PMOS Off
P-L	PMOS Linear
P-S	PMOS Saturation

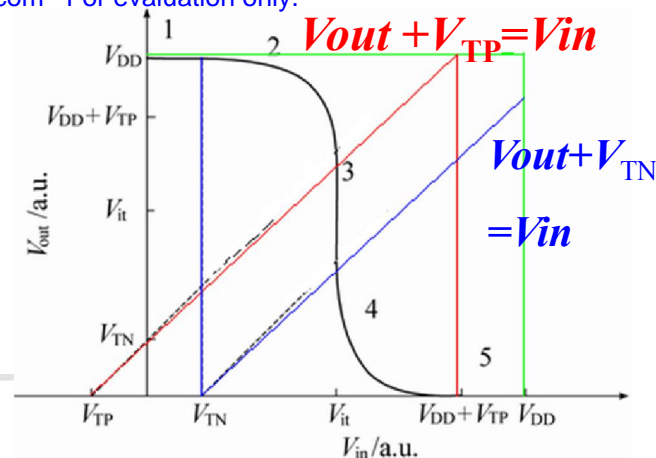


Voltage Transfer Characteristic (VTC)



分析直流特性的出发点：
 直流条件下没有输出电流
 满足： $I_{DN} = I_{DP}$

1、反相器的VTC



1、 $0 \leq V_{in} \leq V_{TN}$

特点: **N-O & P-L**

$$I_{DP} = K_P \left[(V_{in} - V_{TP} - V_{DD})^2 - (V_{in} - V_{TP} - V_{out})^2 \right] = I_{DN} = 0$$

$$V_{out} = V_{DD}, \quad \therefore V_{OH} = V_{DD}$$

2、 $V_{TN} < V_{in} < V_{out} + V_{TP}$

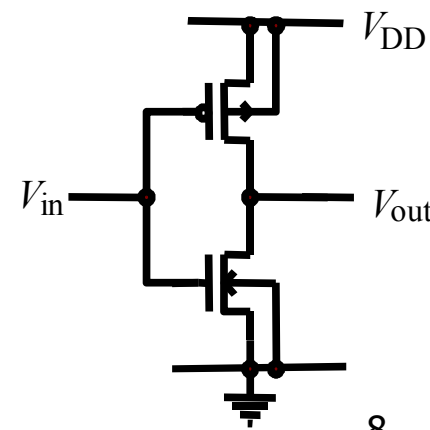
特点: **N-S & P-L**

$$K_P \left[(V_{in} - V_{TP} - V_{DD})^2 - (V_{in} - V_{TP} - V_{out})^2 \right] = K_N (V_{in} - V_{TN})^2$$

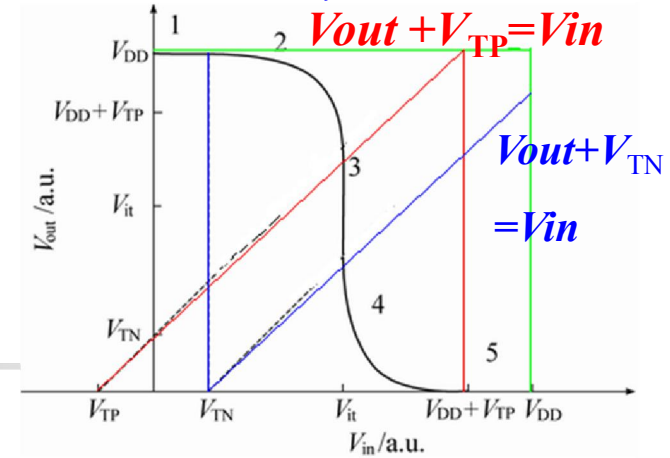
$$V_{out} = (V_{in} - V_{TP}) + \left[(V_{in} - V_{TP} - V_{DD})^2 - K_r (V_{in} - V_{TN})^2 \right]^{1/2}$$

$$K_r = \frac{K_N}{K_P}$$

比例因子



反相器VTC



3、 $V_{out} + V_{TP} \leq V_{in} \leq V_{out} + V_{TN}$ 特点: ***N-S & P-S***

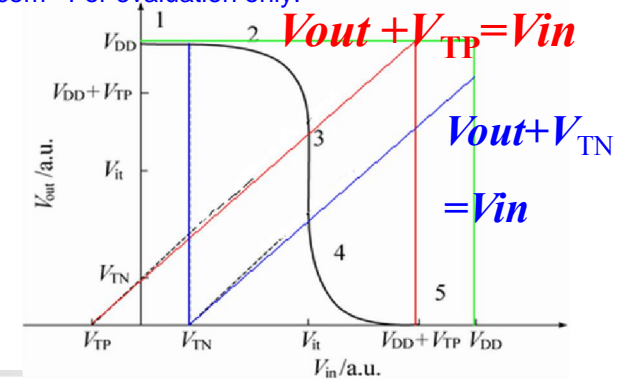
$$K_N (V_{in} - V_{TN})^2 = K_P (V_{in} - V_{TP} - V_{DD})^2$$

$$V_{in} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}}$$

$$V_{it} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}} = \frac{\sqrt{K_r} V_{TN} + V_{DD} + V_{TP}}{1 + \sqrt{K_r}}$$

反相器的逻辑阈值电平（逻辑转折点）

反相器VTC



4、 $V_{out} + V_{TN} < V_{in} < V_{DD} + V_{TP}$

特点: **N-L & P-S**

$$K_N \left[(V_{in} - V_{TN})^2 - (V_{in} - V_{TN} - V_{out})^2 \right] = K_P (V_{in} - V_{TP} - V_{DD})^2$$

$$V_{out} = (V_{in} - V_{TN}) - \left[(V_{in} - V_{TN})^2 - \frac{1}{K_r} (V_{in} - V_{TP} - V_{DD})^2 \right]^{1/2}$$

5、 $V_{DD} \geq V_{in} \geq V_{DD} + V_{TP}$

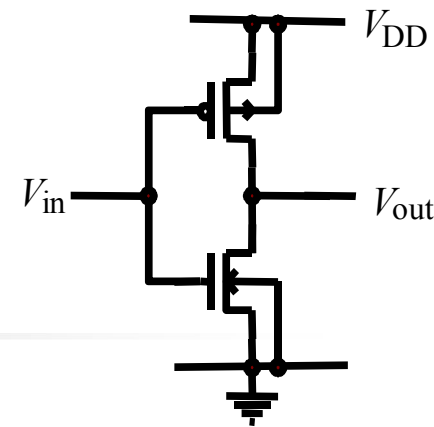
特点: **N-L & P-O**

$$K_N \left[(V_{in} - V_{TN})^2 - (V_{in} - V_{TN} - V_{out})^2 \right] = I_{DP} = 0$$

$$V_{out} = 0 \quad \therefore \quad V_{OL} = 0$$

CMOS反相器实现全摆幅

器件参数对VTC的影响



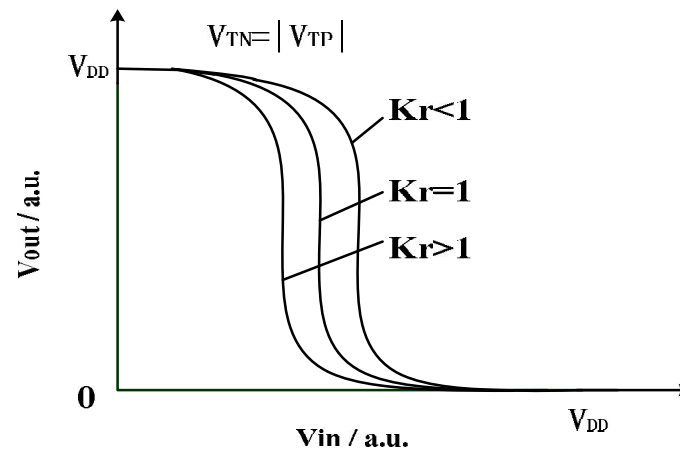
反相器比例因子对直流特性的影响：

在 $V_{TN} = -V_{TP}$ 前提下进行考虑，

以便简化问题；

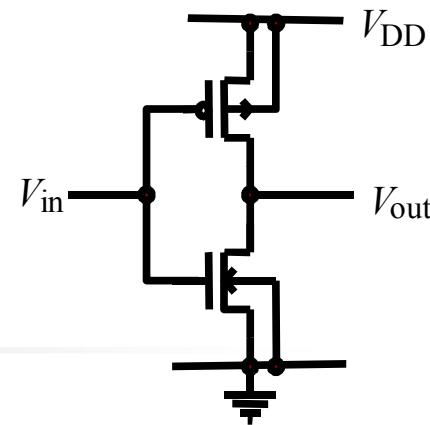
$$V_{in} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}}$$

$$V_{it} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}} = \frac{\sqrt{K_r} V_{TN} + V_{DD} + V_{TP}}{1 + \sqrt{K_r}}$$



(a) 导电因子的影响

器件参数对VTC的影响



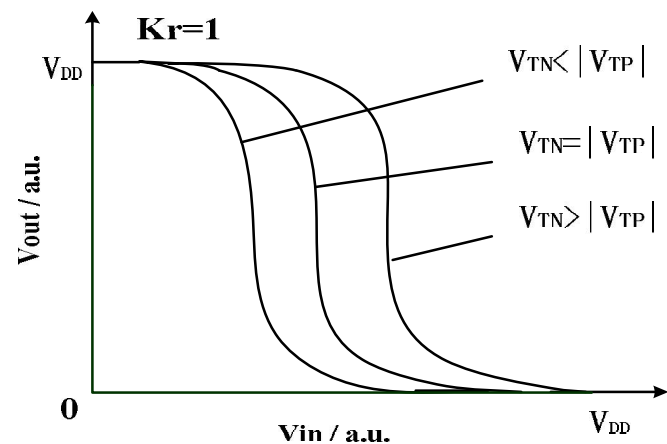
NMOS、PMOS阈值电压的影响；

在**Kr=1**前提下进行考虑，以便简化问题

$$V_{in} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}}$$

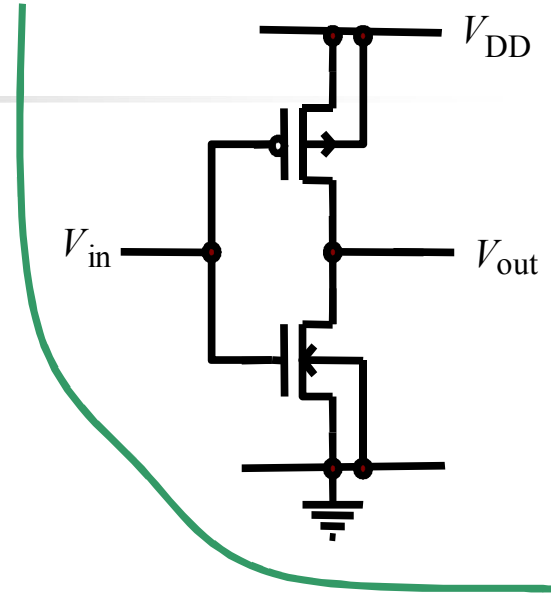
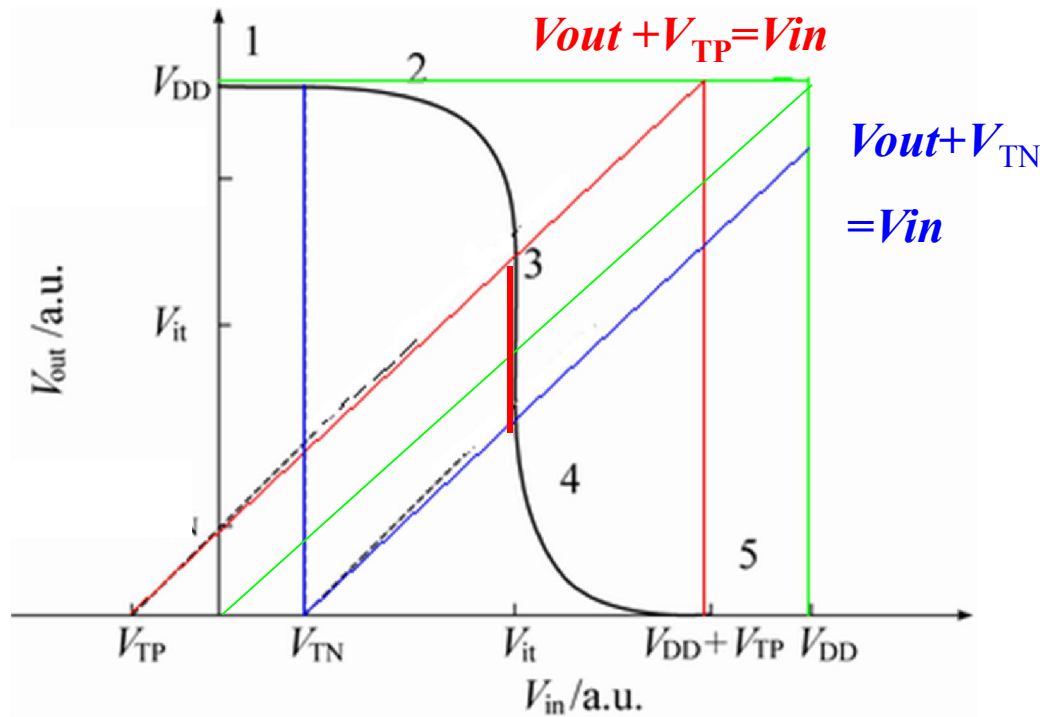
$$V_{it} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}} = \frac{\sqrt{K_r} V_{TN} + V_{DD} + V_{TP}}{1 + \sqrt{K_r}}$$

Y-AXIS



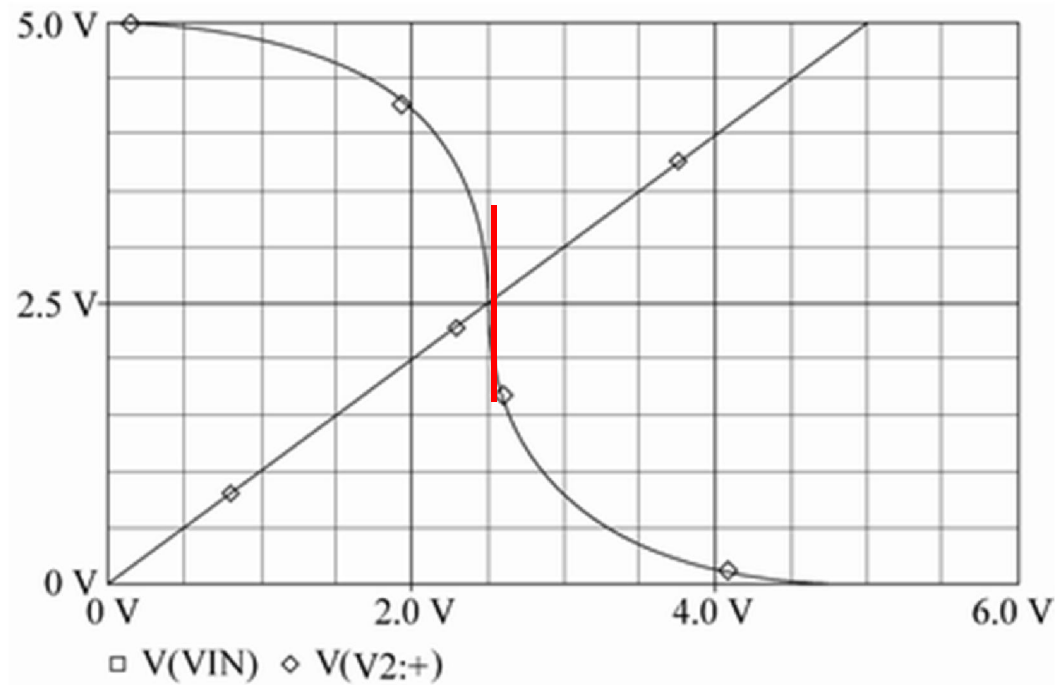
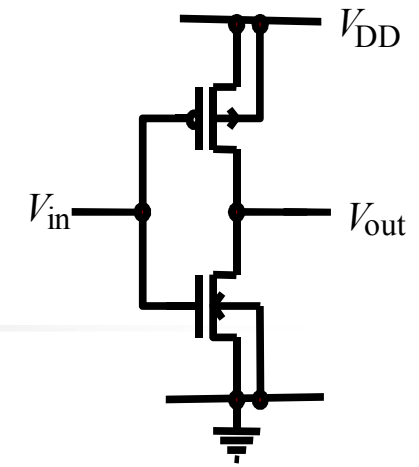
(b) 阈值电压的影响

Voltage Transfer Characteristic (VTC)



3区的高度为两个阈值之和

实际CMOS反相器的VTC



对应 V_{it} 的输入, 输出不是一条垂直线

直流转移特性

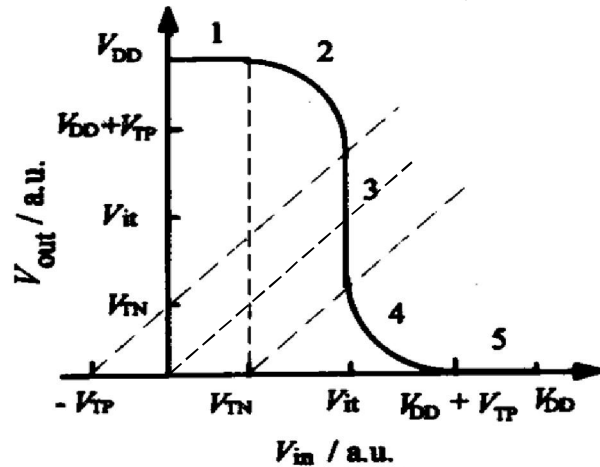
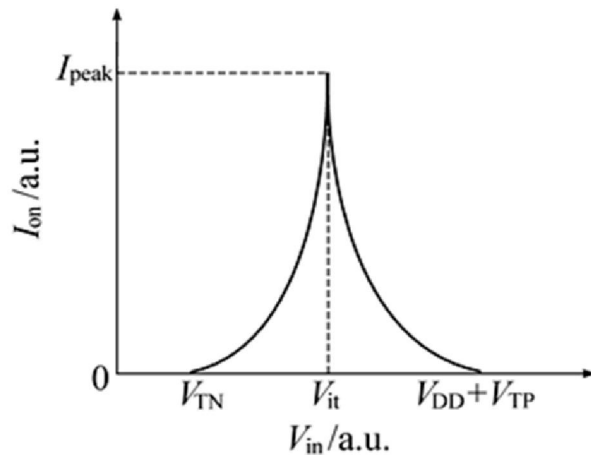


图 4.1.4 理想 CMOS 反相器的直流电压传输特性曲线



分段讨论 Inverter 的导通电流

1. $V_{in} \leq V_{TN}$

$$I_{on} = I_{DN} = I_{DP} = 0,$$

2. $V_{TN} < V_{in} < V_{out} - |V_{TP}|$

$$I_{on} = I_{DN} = I_{DP} \text{ UP}$$

3. $V_{in} = V_{it}$

$$I_{on} = I_{peak} \text{ at } V_{in} = V_{it}$$

4. $V_{out} + V_{TN} < V_{in} < V_{DD} - |V_{TP}|$

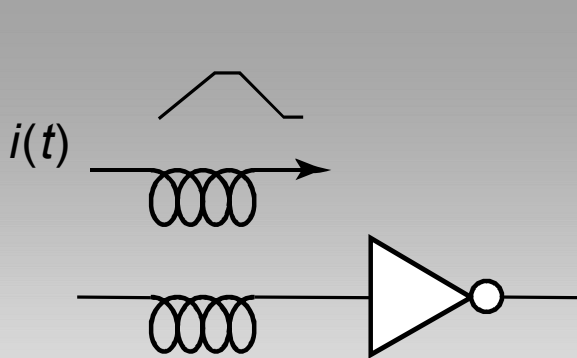
$$I_{on} = I_{DN} = I_{DP} \text{ DOWN}$$

5. $V_{DD} - |V_{TP}| < V_{in} < V_{DD}$

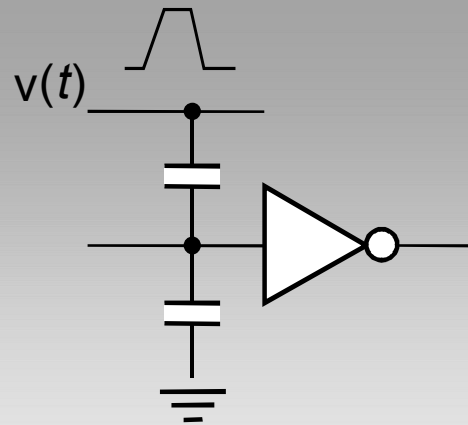
$$I_{on} = I_{DN} = I_{DP} = 0,$$

2、反相器的直流噪声容限

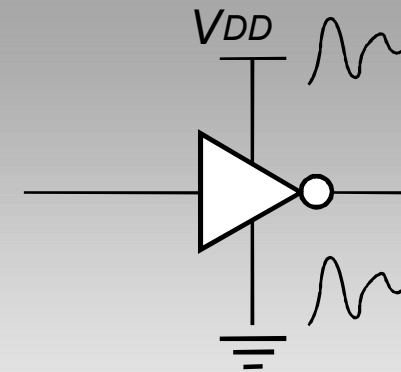
- 数字电路中信号在Vdd和Gnd之间转换，各种干扰信号，可能使得电路中某些结点的信号电平偏离理想电平（Vdd，Gnd），产生所谓的噪声
- 噪声会对电路的可靠性造成影响



Inductive coupling

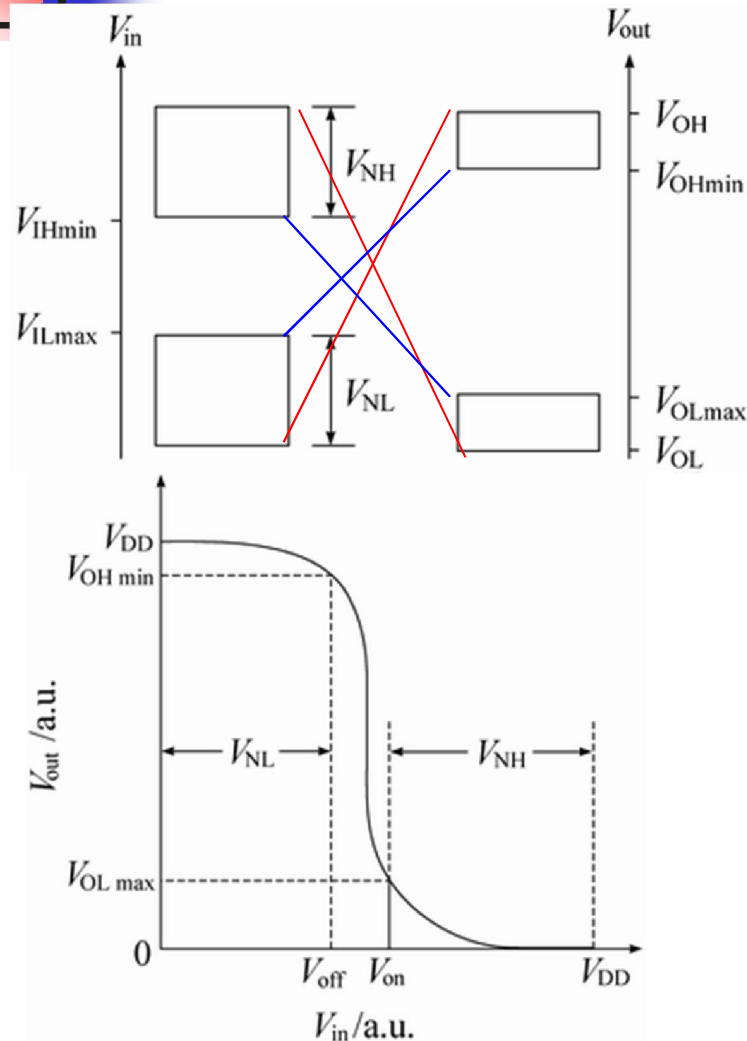


Capacitive coupling



Power and ground noise

反相器噪声容限(Noise Margins)



电路的直流噪声容限——

允许的输入电平变化范围，
反映了电路的抗干扰能力

噪声容限定义1：极限输出

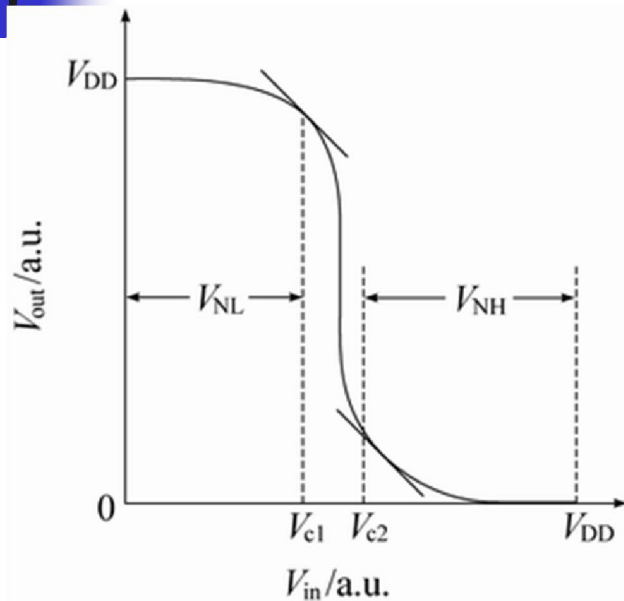
① 给定 V_{OHmin} 和 V_{OLmax}

② $V_{OHmin} \rightarrow V_{off}$ (关门电平)

$V_{OLmax} \rightarrow V_{on}$ (开门电平)

$V_{NL} = V_{off}$, $V_{NH} = V_{DD} - V_{on}$

反相器的直流噪声容限



噪声容限定义**2**：单位增益点

① 在**2、4**区存在

$|dV_{out}/dV_{in}| = 1$ 的

单位增益点

② 在**2、4**区求得增益点对应的 **V_{in}**

(分别为 **V_{c1}** 和 **V_{c2}**),

③ **$V_{NL} = V_{c1}$**

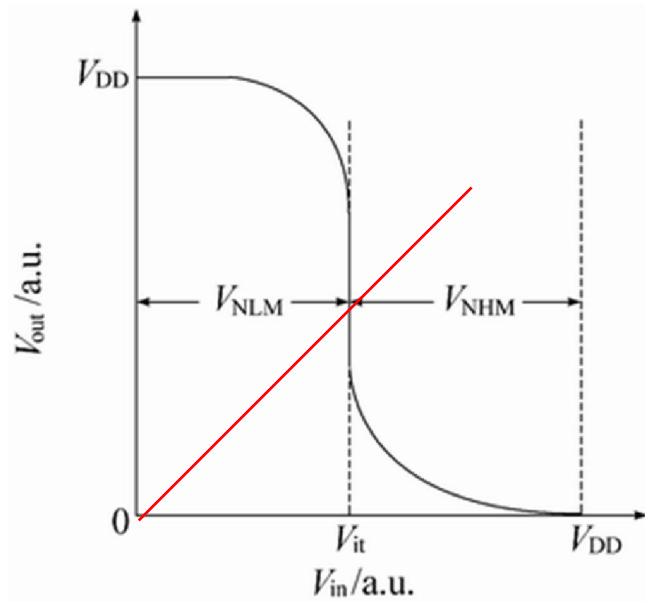
$V_{NH} = V_{DD} - V_{c2}$

$$V_{c1} = \frac{3}{8}V_{DD} + \frac{1}{4}V_T$$

$$V_{c2} = \frac{5}{8}V_{DD} - \frac{1}{4}V_T$$

$$V_{out} = (V_{in} - V_{TP}) + \left[(V_{in} - V_{TP} - V_{DD})^2 - K_r (V_{in} - V_{TN})^2 \right]^{1/2}$$

反相器的直流噪声容限



噪声容限定义**3**：逻辑阈值点

① 把 **V_{it}** 做为允许的输入高电平和低电平极限

② **$V_{NLM} = V_{it}$**

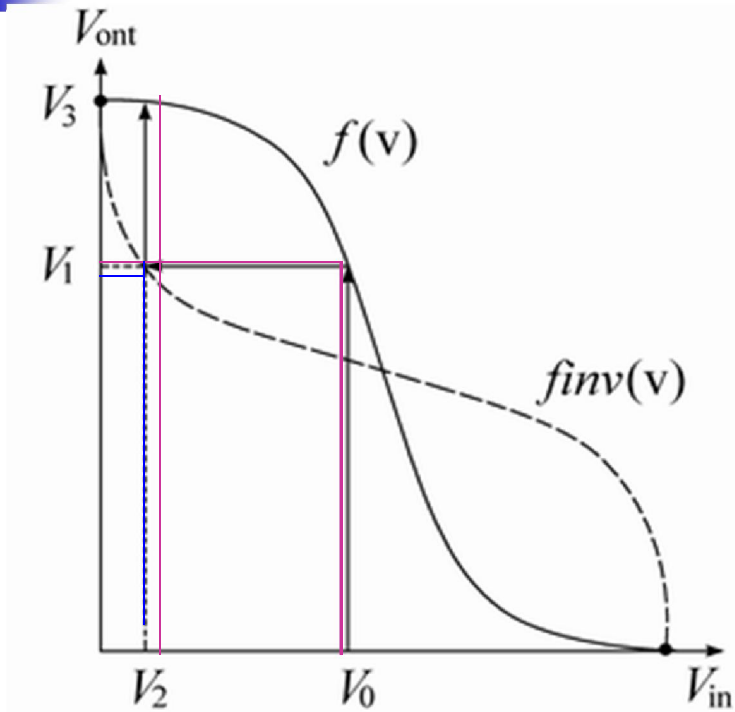
$V_{NHM} = V_{DD} - V_{it}$

③ **V_{NLM} 与 V_{NHM} 中较小的决定最大直流噪声容限**

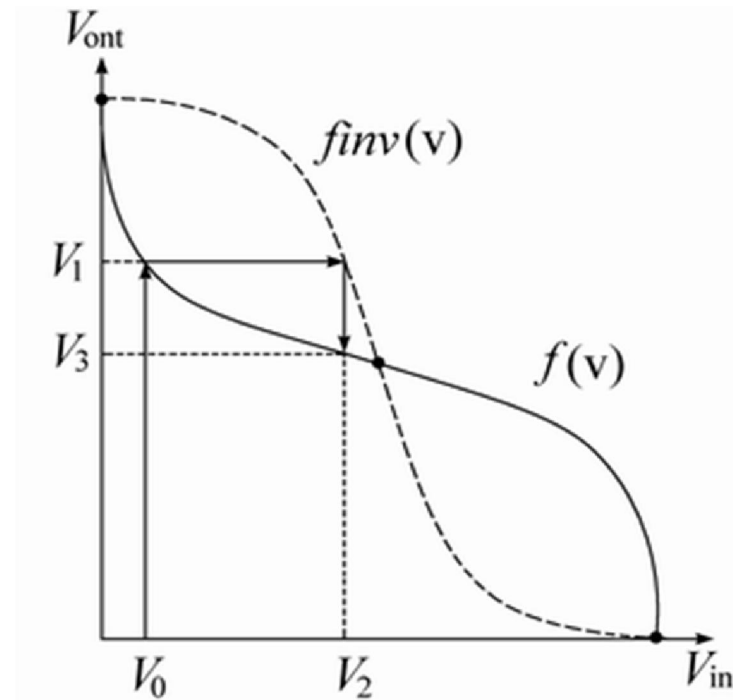
$$V_{in} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}}$$

$$V_{it} = \frac{V_{TN} + \sqrt{1/K_r} (V_{DD} + V_{TP})}{1 + \sqrt{1/K_r}} = \frac{\sqrt{K_r} V_{TN} + V_{DD} + V_{TP}}{1 + \sqrt{K_r}}$$

数字电路具有可恢复逻辑特性



可恢复逻辑特性



不可恢复逻辑特性